



## **School of Computing, Engineering, and the Built Environment Edinburgh Napier University**

### **PHD STUDENT PROJECT**

#### **Application instructions:**

Detailed instructions are available at :

<https://www.napier.ac.uk/research-and-innovation/doctoral-college/how-to-apply>

*Prospective candidates are encouraged to contact the Director of Studies (see details below) to discuss the project and their suitability for it.*

### **Project details**

#### **Supervisory Team:**

- DIRECTOR OF STUDY: Dr Kevin Hughes (Email: [k.hughes@napier.ac.uk](mailto:k.hughes@napier.ac.uk))
- 2<sup>ND</sup> SUPERVISOR: tbc

**Subject Group:** Engineering & Mathematics

**Research Areas:** Mathematics: Pure Mathematics

**Project Title:** Arithmetic and Analysis

#### **Project description:**

This project has multiple options in and between Fourier analysis and analytic number theory. The number theory options build on the recent substantial progress in our understanding of solutions to Diophantine equations in many variables through the use of mean value estimates and the circle method e.g., the use of Vinogradov's mean value theorems in Waring's problem. The Fourier analysis options build on recent progress in maximal functions defined by averages over geometric objects such as curves or hypersurfaces and their ergodic implications. There are many projects that utilise a combination of these ideas and methods in discrete harmonic analysis.

See my seven most recent papers on the arXiv for an idea of what my current interests are: [https://arxiv.org/a/hughes\\_k\\_1.html](https://arxiv.org/a/hughes_k_1.html)

**References:**

- [1] Stein & Shakarchi's Princeton Lectures in Analysis (Fourier Analysis, Complex Analysis and Real Analysis)
- [2] Analysis and Real Analysis)
- [3] Tao's notes on Fourier analysis (see <https://www.math.ucla.edu/~tao/247a.1.06f/>)
- [4] Hardy & Wright's An Introduction to the Theory of Numbers
- [5] Davenport's Analytic Methods in Diophantine equations and Diophantine inequalities
- [6] Vaughan The Hardy--Littlewood Method

## **Candidate characteristics**

**Education:**

A first-class honours degree, or a distinction at master level, or equivalent achievements in Pure Mathematics

**Subject knowledge:**

- Fourier analysis
- Number theory
- Harmonic analysis

**Essential attributes:**

- Experience of fundamental pure mathematics including real analysis, complex function theory
- and basic number theory
- Competent in pure mathematics at the undergraduate level
- Knowledge of Pure Mathematics including analysis
- Good written and oral communication skills
- Strong motivation, with evidence of independent research skills relevant to the project
- Good time management

**Desirable attributes:**

- Desire to learn any topics you are unfamiliar with and to undertake long-term research projects.